

ECEN 667

Power System Stability

Lecture 9: Synchronous Machine Modeling

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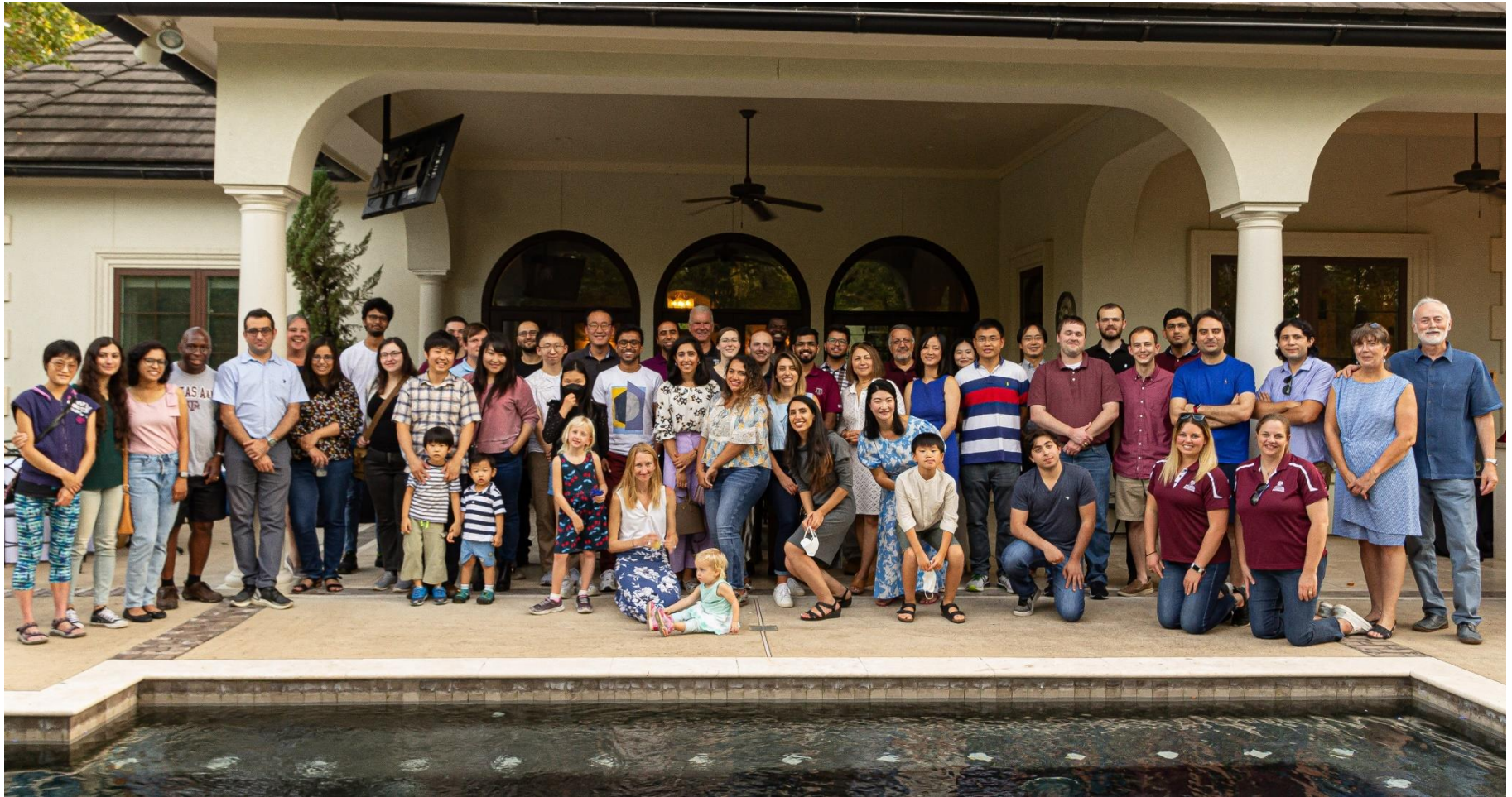
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Announcements



- Read Chapter 5
- Homework 3 is due on Thursday Oct 7
 - Good writing is a key engineering skill! I like, *The Handbook of Technical Writing* by Alred, Brusaw and Oliu (now in the 12th Edition)
- Homework 4 will be assigned on Sept 30, but will not need to be turned in (just done before the first exam)
- Exam 1 will be on Oct 14 in class
 - For the distance learners we usually use Honorlock (though I know for some that won't work)
 - Exams are closed book, closed notes, but you can bring in one 8.5 by 11 inch note sheet and can use calculators

EPG Group Dinner, Sep 25, 2021



Two-Axis Model



$$T'_{do} \frac{dE'_q}{dt} = -E'_q - (X_d - X'_d)I_d + E_{fd}$$

$$T'_{qo} \frac{dE'_d}{dt} = -E'_d + (X_q - X'_q)I_q$$

$$\frac{d\delta}{dt} = \omega - \omega_s$$

$$\frac{2H}{\omega_s} \frac{d\omega}{dt} = T_M - E'_d I_d - E'_q I_q - (X'_q - X'_d) I_d I_q - T_{FW}$$

$$0 = (R_s + R_e)I_d - (X'_q + X_{ep})I_q - E'_d + V_s \sin(\delta - \theta_{vs})$$

$$0 = (R_s + R_e)I_q + (X'_d + X_{ep})I_d - E'_q + V_s \cos(\delta - \theta_{vs}) \setminus$$

$$V_d = R_e I_d - X_{ep} I_q + V_s \sin(\delta - \theta_{vs})$$

$$V_q = R_e I_q + X_{ep} I_d + V_s \cos(\delta - \theta_{vs})$$

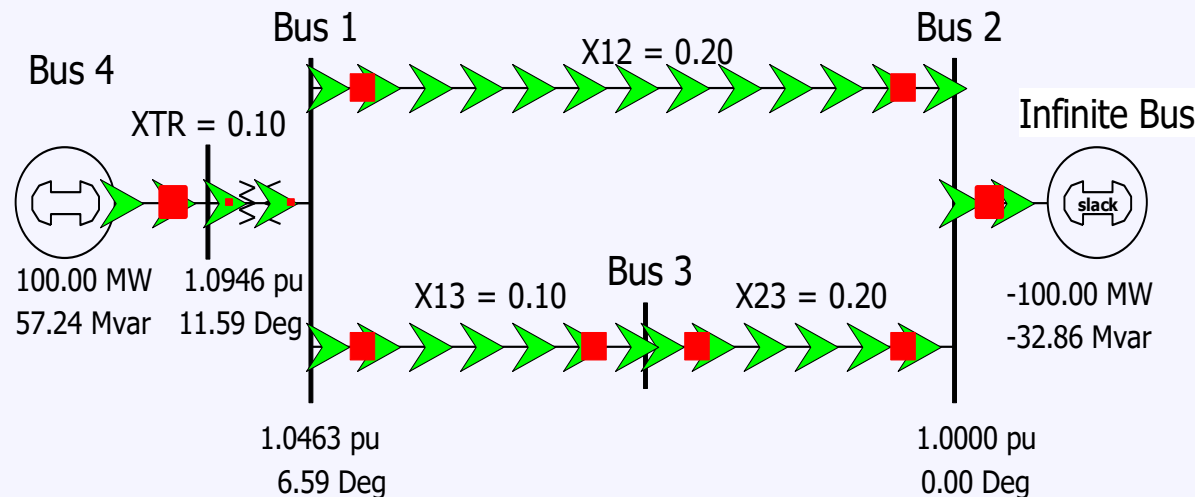
$$V_t = \sqrt{V_d^2 + V_q^2}$$

No saturation effects are included with this model

Example (Used for All Models)



- Below example will be used with all models. Assume a 100 MVA base, with gen supplying $1.0+j0.3286$ power into infinite bus with unity voltage through network impedance of $j0.22$
 - Gives current of $1.0 - j0.3286 = 1.0526 \angle -18.19^\circ$
 - Generator terminal voltage of $1.072+j0.22 = 1.0946 \angle 11.59^\circ$



Sign convention on current is out of the generator is positive

Two-Axis Example



- For the two-axis model assume $H = 3.0$ per unit-seconds, $R_s = 0$, $X_d = 2.1$, $X_q = 2.0$, $X'_d = 0.3$, $X'_q = 0.5$, $T'_{do} = 7.0$, $T'_{qo} = 0.75$ per unit using the 100 MVA base.
- Solving we get

$$\bar{E} = 1.0946 \angle 11.59^\circ + (j2.0)(1.0526 \angle -18.19^\circ) = 2.81 \angle 52.1^\circ$$

$$\rightarrow \delta = 52.1^\circ$$

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.0723 \\ 0.220 \end{bmatrix} = \begin{bmatrix} 0.7107 \\ 0.8326 \end{bmatrix}$$

$$\begin{bmatrix} I_d \\ I_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.000 \\ -0.3287 \end{bmatrix} = \begin{bmatrix} 0.9909 \\ 0.3553 \end{bmatrix}$$

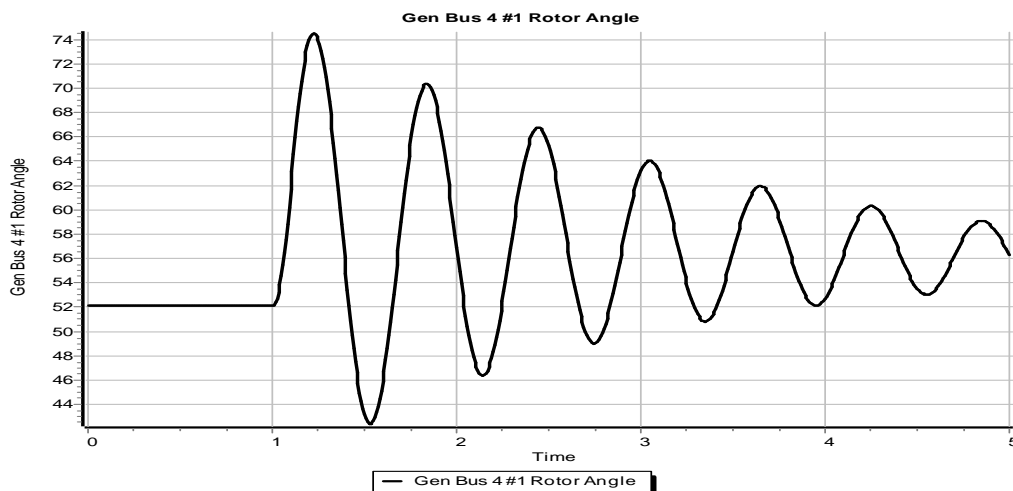
Two-Axis Example



- And $E'_q = 0.8326 + (0.3)(0.9909) = 1.130$
 $E'_d = 0.7107 - (0.5)(0.3553) = 0.533$
 $E_{fd} = 1.1299 + (2.1 - 0.3)(0.9909) = 2.913$

Saved as case **B4_TwoAxis**

- Assume a fault at bus 3 at time $t=1.0$, cleared by opening both lines into bus 3 at time $t=1.1$ seconds



Two-Axis Example



- PowerWorld allows the gen states to be easily stored

Result Storage

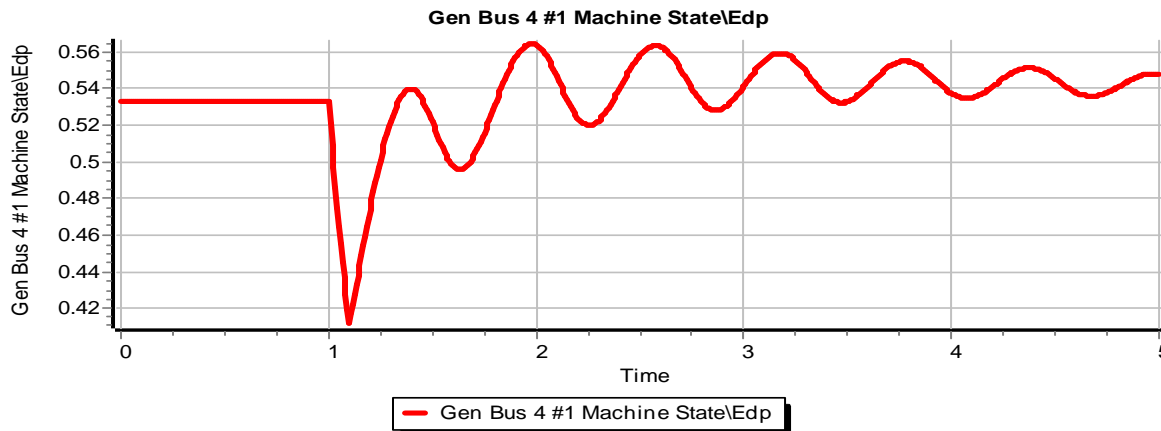
Where to Save/Store Results: Save Results Every n Timesteps: Store Results to RAM Save Results to Hard Drive Do Not Combine RAM Results with Hard Drive Results Save the Results stored to RAM in the PWB file Save the Min/Max Results stored to RAM in the PWB file

Store to RAM Options | Save to Hard Drive Options

Note: All fields that are specified in a plot series of defined plot will also be stored to RAM.

Store Results for Open Devices

Generator	Bus	Load	Switched Shunt	Branch	Transformer	DC Transmission Line	VSC DC Line	Multi-Terminal DC Record	Multi-Terminal DC Converter	Area	Zone	Interf						
From Selection:	Save All	Save Rotor Angle	Save Rotor Angle No Shift	Save Speed	Save MW Mech	Save MW	Save MW Accel	Save Mvar	Save V pu	Save Efd	Save Ifd	Save Vstab	Save VOEL	Save VUEL	Save I pu	Save Status	Save Machine State	Save Exciter State
Make Plot	1 NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO	NO
Make Plot	2 NO	YES	NO	YES	NO	YES	NO	YES	NO	NO	NO	NO	NO	NO	NO	NO	YES	NO



Graph shows variation in E_d'

Flux Decay Model



- If we assume T'_{q0} is sufficiently fast that its equation becomes an algebraic constraint

$$T'_{q0} \frac{dE'_d}{dt} = -E'_d + (X_q - X'_q) I_q = 0$$

In previous example
 $T'_{q0} = 0.75$

$$T'_{d0} \frac{dE'_q}{dt} = -E'_q - (X_d - X'_d) I_d + E_{fd}$$

$$\frac{d\delta}{dt} = \omega - \omega_s$$

$$\frac{2H}{\omega_s} \frac{d\omega}{dt} = T_M - E'_d I_d - E'_q I_q - (X'_q - X'_d) I_d I_q - T_{FW}$$

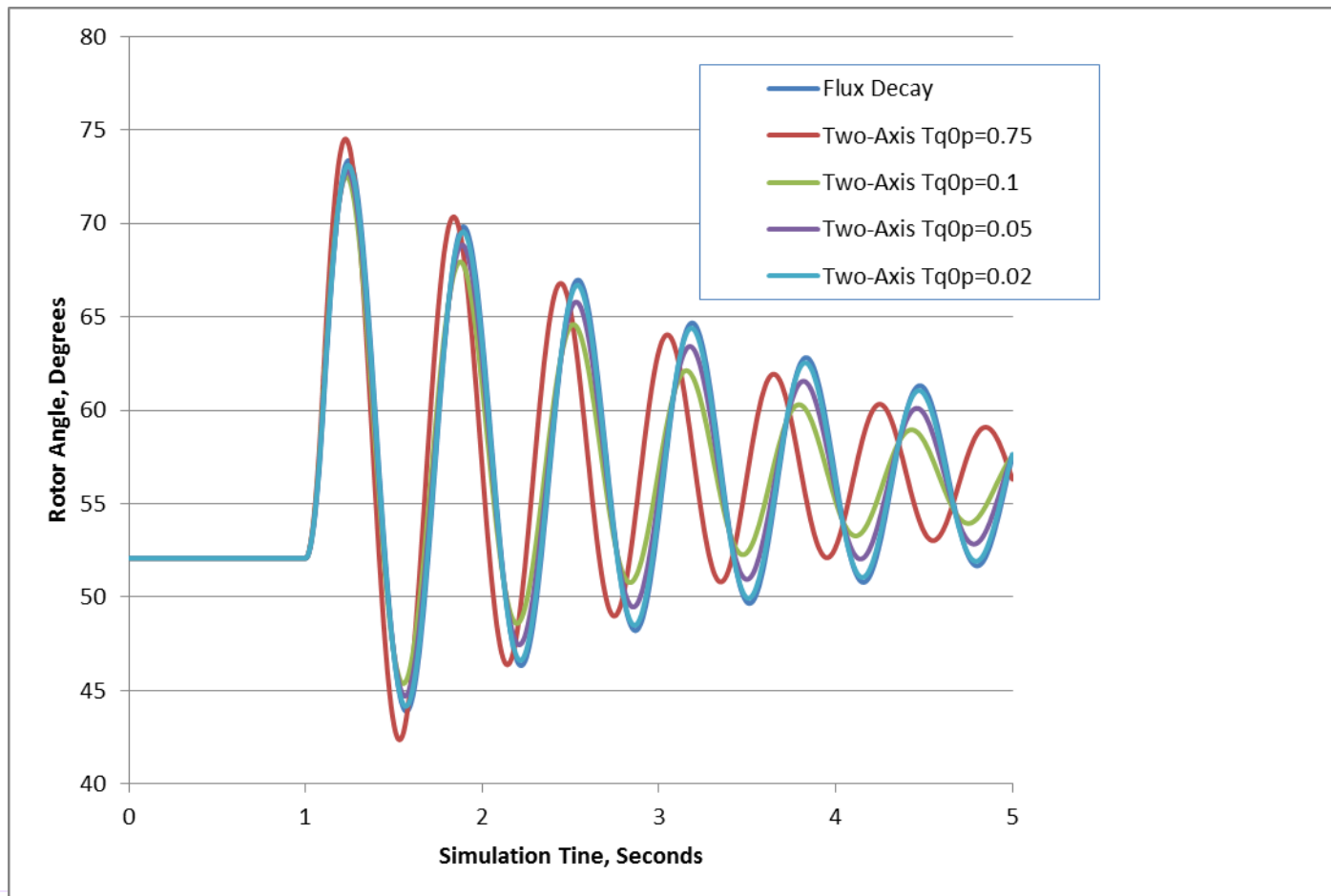
$$= T_M - (X_q - X'_q) I_q I_d - E'_q I_q - (X'_q - X'_d) I_d I_q - T_{FW}$$

$$= T_M - E'_q I_q - (X_q - X'_d) I_d I_q - T_{FW}$$

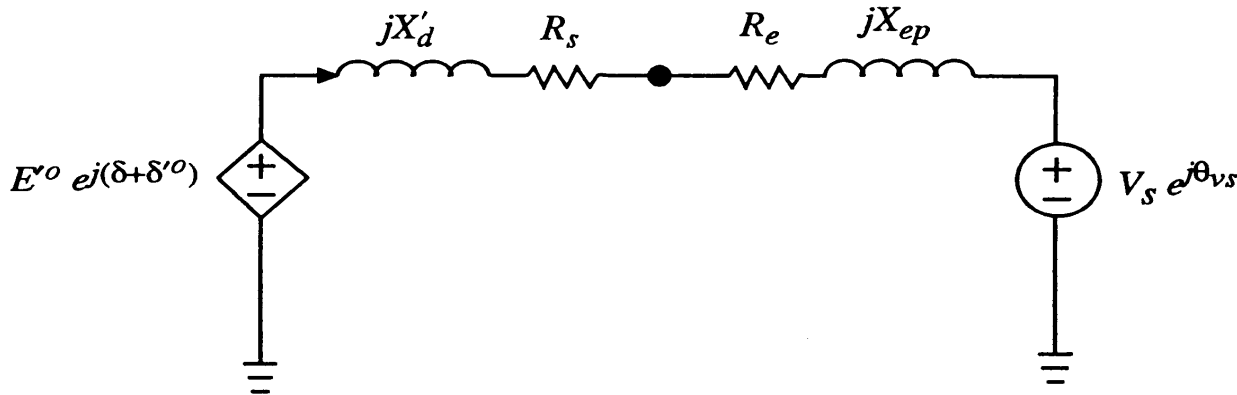
Rotor Angle Sensitivity to Tqop



- Graph shows variation in the rotor angle as Tqop is varied, showing the flux decay is the same as Tqop = 0



Classical Model



$$\frac{d\delta}{dt} = \omega - \omega_s$$

$$\frac{2H}{\omega_0} \frac{d\omega}{dt} = T_M^0 - \frac{E'^0 V_s}{X'_d + X_{ep}} \sin(\delta - \theta_{vs}) - T_{FW}$$

This is a pendulum model

The classical model had been widely used because it is simple. At best it can only approximate a very short term response. It is no longer common.

Classical Model Justification



- It is difficult to justify. One approach would be to go from the flux decay model and assume

$$X_q = X'_d \quad T'_{do} = \infty$$

$$E' = E'_q \quad \delta'^0 = 0$$

- Or go back to the two-axis model and assume

$$X'_q = X'_d \quad T'_{do} = \infty \quad T'_{qo} = \infty$$

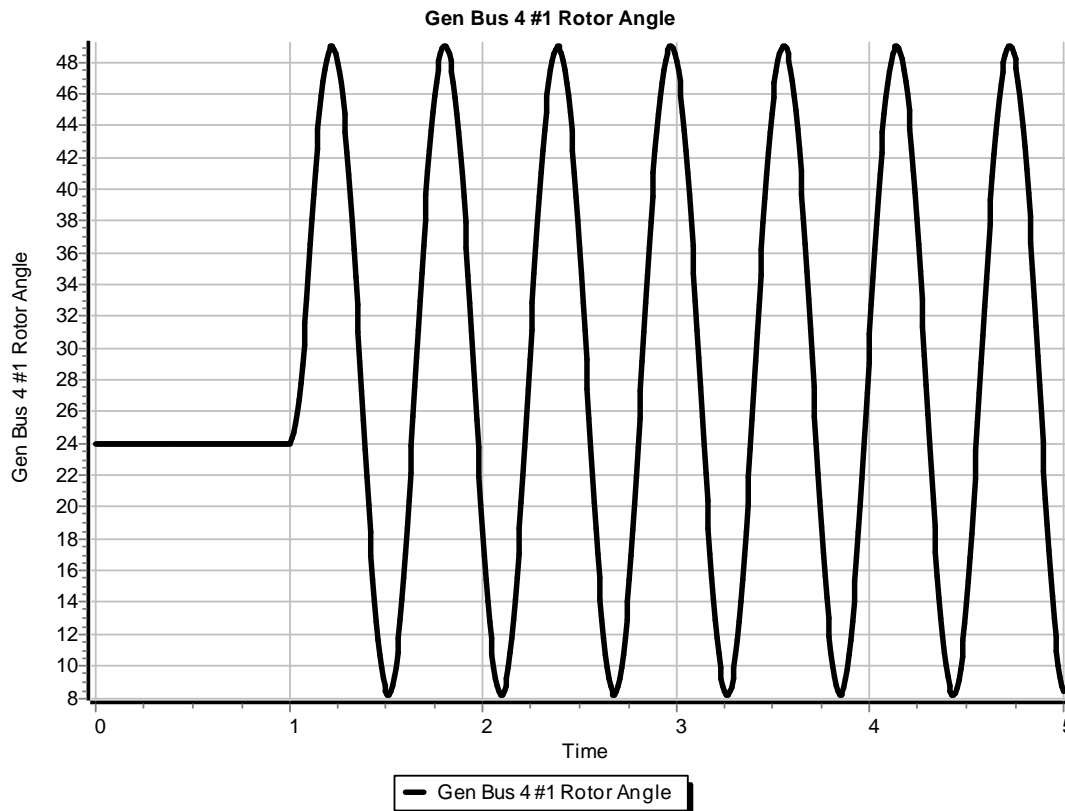
$$E' = \sqrt{E_q'^0{}^2 + E_d'^0{}^2} \quad (E_q' = \text{const} \quad E_d' = \text{const})$$

$$\delta'^0 = \tan^{-1} \left(\frac{E_q'^0}{E_d'^0} \right) - \pi/2$$

Classical Model Response



- Rotor angle variation for same fault as before



Notice that even though the rotor angle is quite different, its initial increase (of about 24 degrees) is similar. However there is no damping.

Saved as case **B4_GENCLS**

Subtransient Models



- The two-axis model is a transient model
- Essentially all commercial studies now use subtransient models
- First models considered are GENSAL and GENROU, which require $X''_d = X''_q$
- This allows the internal, subtransient voltage to be represented as

$$\bar{E}'' = \bar{V} + (R_s + jX'')\bar{I}$$

$$E''_d + jE''_q = (-\psi''_q + j\psi''_d)\omega$$

Subtransient Models



- Usually represented by a Norton Injection with

$$I_d + jI_q = \frac{E_d'' + jE_q''}{R_s + jX''} = \frac{(-\psi_q'' + j\psi_d'')\omega}{R_s + jX''}$$

- May also be shown as

$$-j(I_d + jI_q) = I_q - jI_d = \frac{-j(-\psi_q'' + j\psi_d'')\omega}{R_s + jX''} = \frac{(\psi_d'' + j\psi_q'')\omega}{R_s + jX''}$$

In steady-state $\omega = 1.0$

Standards



- Standards play important roles in many aspects of engineering analysis by providing public (though often not free) access to standard models and other things (such as data formats)
 - Standards can be updated
- The standards are then used by manufacturers (and others) to create compatible products
- However, manufacturers do not need to always follow the standards



IEEE Guide for Synchronous Generator Modeling Practices and Parameter Verification with Applications in Power System Stability Analyses

IEEE Power and Energy Society

Developed by the
Electric Machinery Committee

IEEE Std 1110™-2019
(Revision of IEEE Std 1110-2002)



STANDARDS

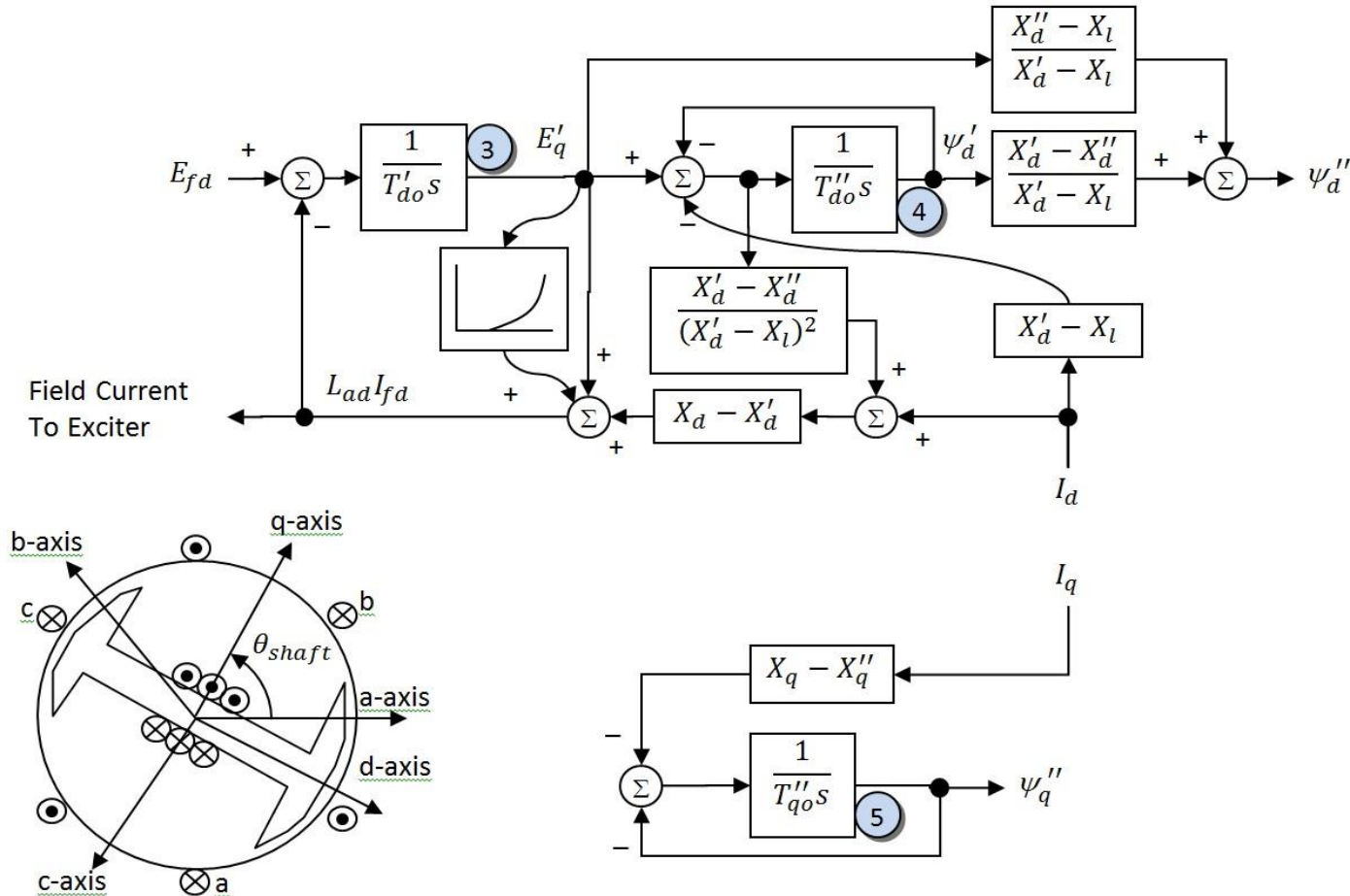
GENSAL



- The GENSAL model had been widely used to model salient pole synchronous generators
 - In salient pole models saturation is only assumed to affect the d-axis
 - In the 2010 WECC cases about 1/3 of machine models were GENSAL; in 2013 essentially none are, being replaced by GENTPF or GENTPJ
 - A 2014 series EI model had about 1/3 of its machines models set as GENSAL
 - In November 2016 NERC issued a recommendation to use GENTPJ rather than GENSAL for new models. See

www.nerc.com/comm/PC/NERCModelingNotifications/Use%20of%20GENTPJ%20Generator%20Model.pdf

GENSAL Block Diagram



A quadratic saturation function is used; for initialization it only impacts the E_{fd} value

GENSAL Example



- Assume same system as before with same common generator parameters: $H=3.0$, $D=0$, $R_a = 0$, $X_d = 2.1$, $X_q = 2.0$, $X'_d = 0.3$, $X''_d=X''_q=0.2$, $X_l = 0.13$, $T'_{do} = 7.0$, $T''_{do} = 0.07$, $T''_{qo} = 0.07$, $S(1.0) = 0$, and $S(1.2) = 0$.
- Same terminal conditions as before
 - Current of $1.0-j0.3286$ and generator terminal voltage of $1.072+j0.22 = 1.0946 \angle 11.59^\circ$
- Use same equation to get initial δ

Same delta as with the other models

$$\begin{aligned} |E| \angle \delta &= \bar{V} + (R_s + jX_q) \bar{I} \\ &= 1.072 + j0.22 + (0.0 + j2)(1.0 - j0.3286) \\ &= 1.729 + j2.22 = 2.81 \angle 52.1^\circ \end{aligned}$$

Saved as case
B4_GENSAL

GENSAL Example



- Then as before

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.0723 \\ 0.220 \end{bmatrix} = \begin{bmatrix} 0.7107 \\ 0.8326 \end{bmatrix}$$

$$\text{and } \begin{bmatrix} I_d \\ I_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.000 \\ -0.3287 \end{bmatrix} = \begin{bmatrix} 0.9909 \\ 0.3553 \end{bmatrix}$$

$$\bar{V} + (R_s + jX'')\bar{I}$$

$$= 1.072 + j0.22 + (0 + j0.2)(1.0 - j0.3286)$$

$$= 1.138 + j0.42$$

GENSAL Example



- Giving the initial fluxes (with $\omega = 1.0$) of

$$\begin{bmatrix} -\psi_q'' \\ \psi_d'' \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.138 \\ 0.420 \end{bmatrix} = \begin{bmatrix} 0.6396 \\ 1.031 \end{bmatrix}$$

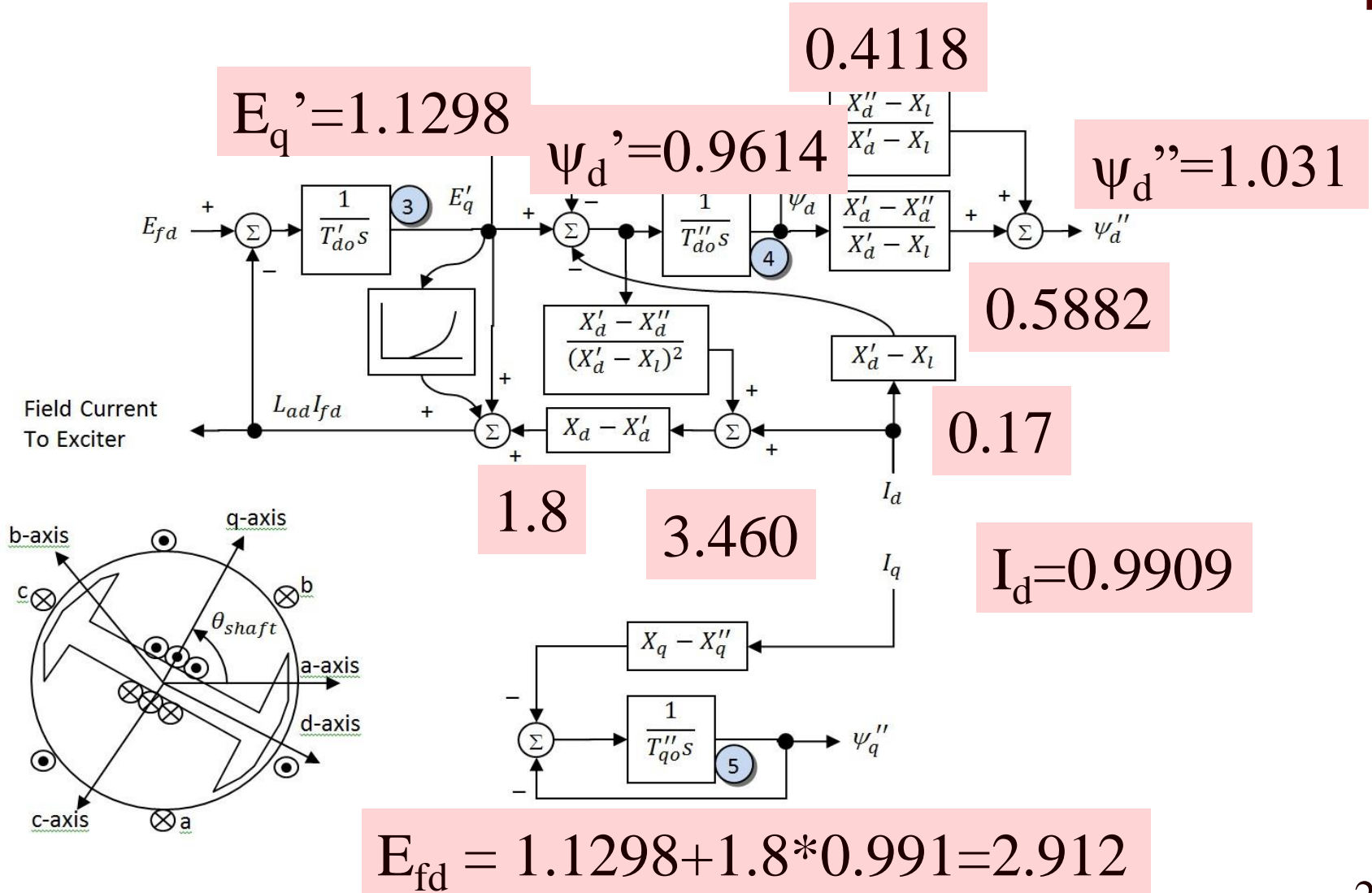
- To get the remaining variables set the differential equations equal to zero, e.g.,

$$\psi_q'' = -(X_q - X_q'')I_q = -(2 - 0.2)(0.3553) = -0.6396$$

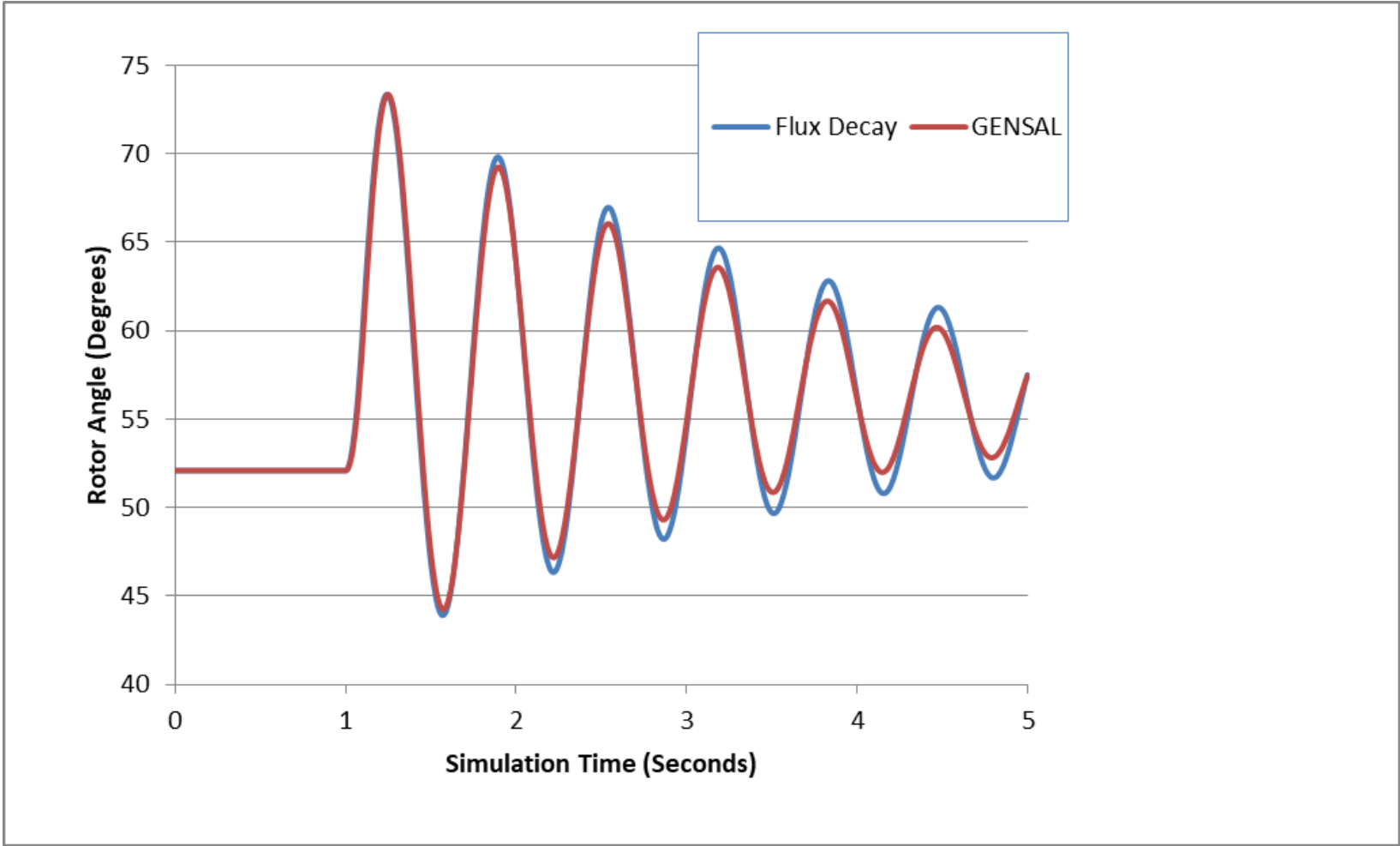
$$E_q' = 1.1298, \quad \psi_d' = 0.9614$$

Solving the d-axis requires solving two linear equations for two unknowns

GENSAL Example



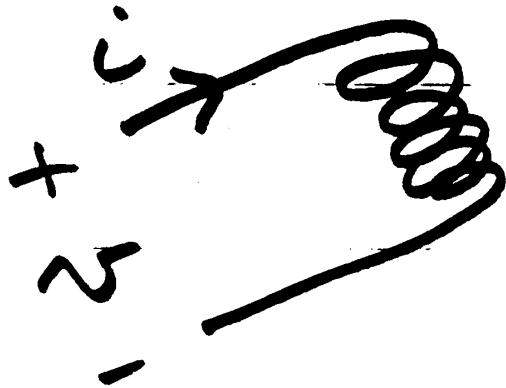
Comparison Between Gensal and Flux Decay



Nonlinear Magnetic Circuits



- Nonlinear magnetic models are needed because magnetic materials tend to saturate; that is, increasingly large amounts of current are needed to increase the flux density

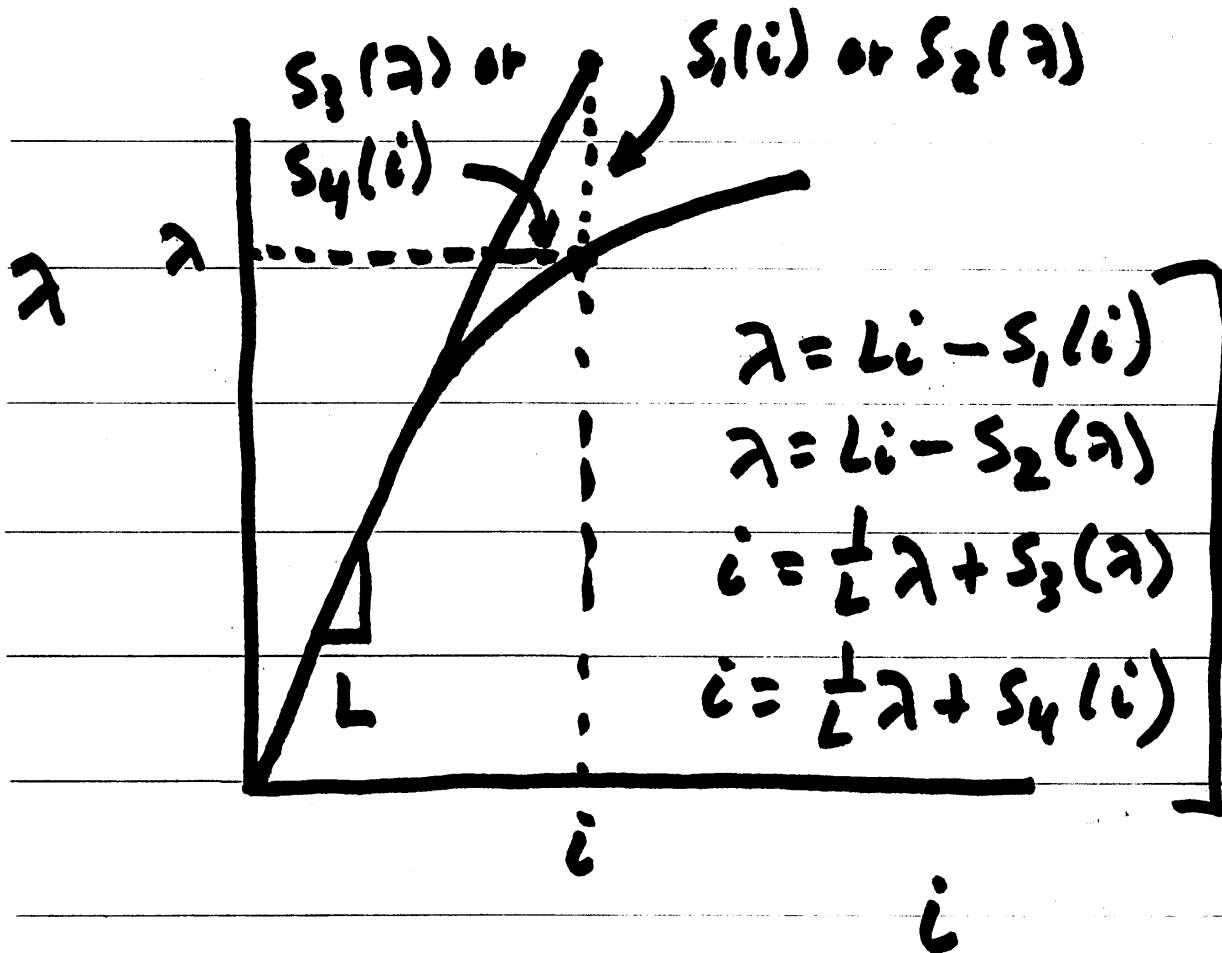


$$R = 0$$

$$v = \frac{d\lambda}{dt} = N \frac{d\phi}{dt}$$

When linear $\lambda = Li$

Saturation



Relative Magnetic Strength Levels

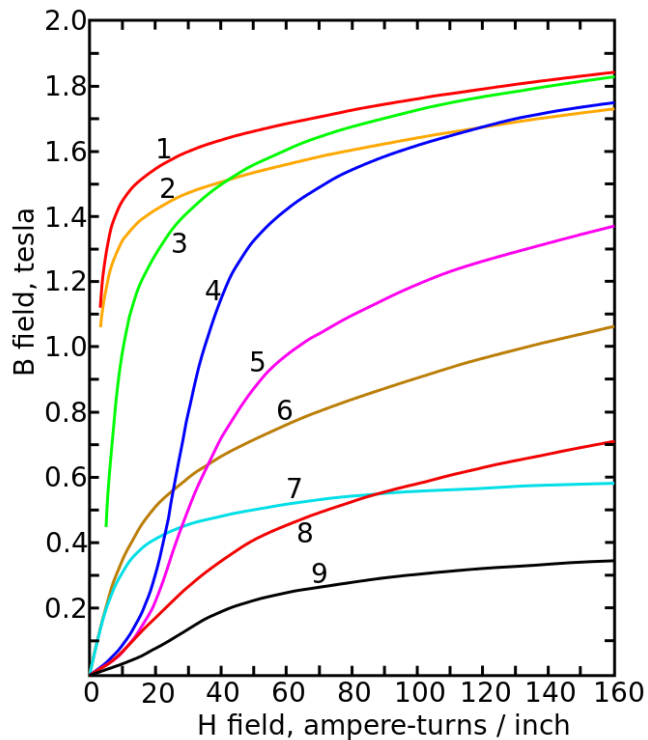


- Earth's magnetic field is between 30 and 70 μT (0.3 to 0.7 gauss)
- A refrigerator magnet might have 0.005 T
- A commercial neodymium magnet might be 1 T
- A magnetic resonance imaging (MRI) machine would be between 1 and 3 T
- Strong lab magnets can be 10 T
- Frogs can be levitated at 16 T
www.ru.nl/hfml/research/levitation/diamagnetic-levitation/
- A neutron star can have 1 to 100 MT!

Magnetic Saturation and Hysteresis



- The below image shows the saturation curves for various materials



Magnetization curves of 9 ferromagnetic materials, showing saturation. 1. Sheet steel, 2. Silicon steel, 3. Cast steel, 4. Tungsten steel, 5. Magnet steel, 6. Cast iron, 7. Nickel, 8. Cobalt, 9. Magnetite; highest saturation materials can get to around 2.2 or 2.3T

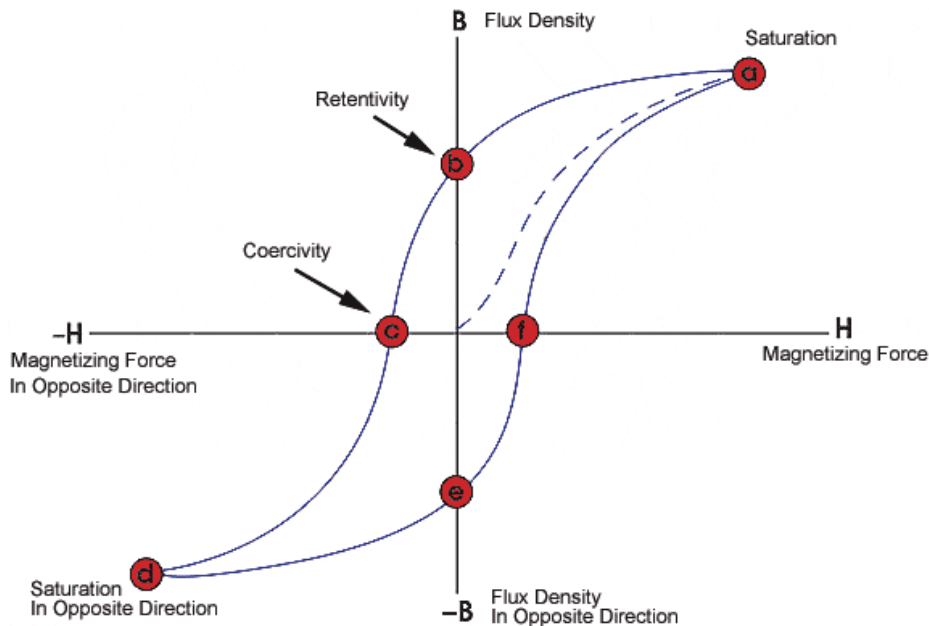
H is proportional to current

Image Source: [en.wikipedia.org/wiki/Saturation_\(magnetic\)](https://en.wikipedia.org/wiki/Saturation_(magnetic))

Magnetic Saturation and Hysteresis



- Magnetic materials also exhibit hysteresis, so there is some residual magnetism when the current goes to zero; design goal is to reduce the area enclosed by the hysteresis loop



To minimize the amount of magnetic material, and hence cost and weight, electric machines are designed to operate close to saturation

Saturation Models



- Many different models exist to represent saturation
 - There is a tradeoff between accuracy and complexity
- One simple approach is to replace

$$\frac{dE'_q}{dt} = \frac{1}{T'_{do}} \left(-E'_q - (X_d - X'_d)I_d + E_{fd} \right)$$

- with

$$\frac{dE'_q}{dt} = \frac{1}{T'_{do}} \left(-E'_q - (X_d - X'_d)I_d - Se(E'_q) + E_{fd} \right)$$

Saturation Models



- In steady-state this becomes

$$E_{fd} = E'_q + (X_d - X'_d)I_d + Se(E'_q)$$

- Hence saturation increases the required E_{fd} to get a desired flux
- Saturation is usually modeled using a quadratic function, with the value of Se specified at two points (often at 1.0 flux and 1.2 flux)

$$Se = B(E'_q - A)^2$$

An alternative model is
$$Se = \frac{B(E'_q - A)^2}{E'_q}$$

A and B are determined from two provided data points

Saturation Example



- If $Se = 0.1$ when the flux is 1.0 and 0.5 when the flux is 1.2, what are the values of A and B using the

$$Se = B(E'_q - A)^2$$

To solve use the $Se(1.2)$ value to eliminate B

$$B = \frac{Se(1.2)}{(1.2 - A)^2} \rightarrow Se(1.0) = \frac{Se(1.2)}{(1.2 - A)^2} (1.0 - A)^2$$

$$(1.2 - A)^2 Se(1.0) = Se(1.2)(1.0 - A)^2$$

With the values we get

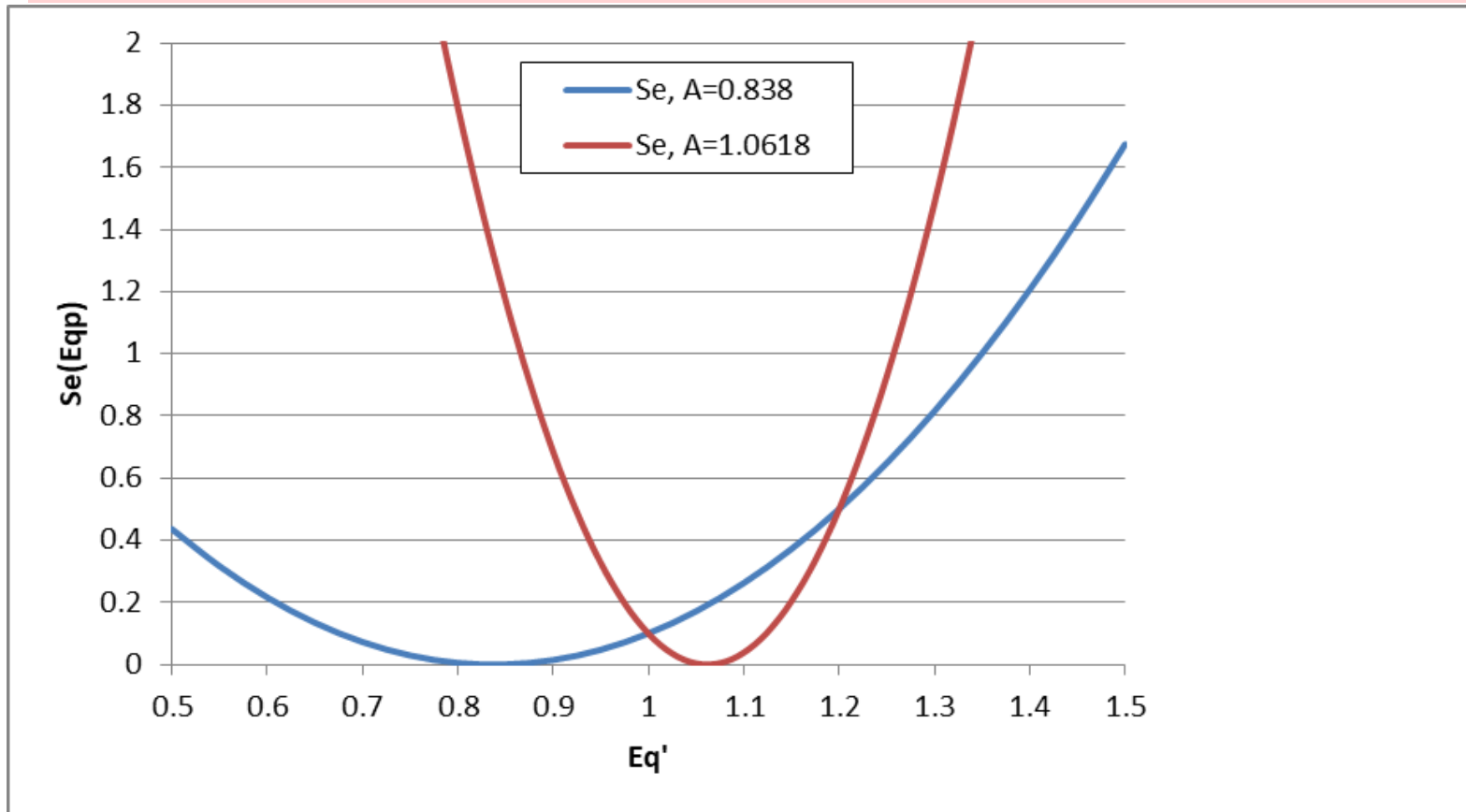
$$4A^2 - 7.6A + 3.56 = 0 \rightarrow A = 0.838 \text{ or } 1.0618$$

Use $A=0.838$, which gives $B=3.820$

Saturation Example: Selection of A



When selecting which of the two values of A to use, we do not want the minimum to be between the two specified values. That is $Se(1.0)$ and $Se(1.2)$.



Implementing Saturation Models



- When implementing saturation models in code, it is important to recognize that the function is meant to be positive, so negative values are not allowed
- In large cases one is almost guaranteed to have special cases, sometimes caused by user typos
 - What to do if $Se(1.2) < Se(1.0)$?
 - What to do if $Se(1.0) = 0$ and $Se(1.2) \neq 0$
 - What to do if $Se(1.0) = Se(1.2) \neq 0$
- Exponential saturation models have also been used

GENSAL Example with Saturation



- Once E'_q has been determined, the initial field current (and hence field voltage) are easily determined by recognizing in steady-state the E'_q is zero

$$\begin{aligned} E_{fd} &= E'_q \left(1 + Sat(E'_q) \right) + (X_d - X'_d) I_D \\ &= 1.1298 \left(1 + B(1.1298 - A)^2 \right) + (2.1 - 0.3)(0.9909) \\ &= 1.1298 \left(1 + 3.82(1.1298 - 0.838)^2 \right) + 1.784 = 3.28 \end{aligned}$$

Saturation coefficients were determined from the two initial values

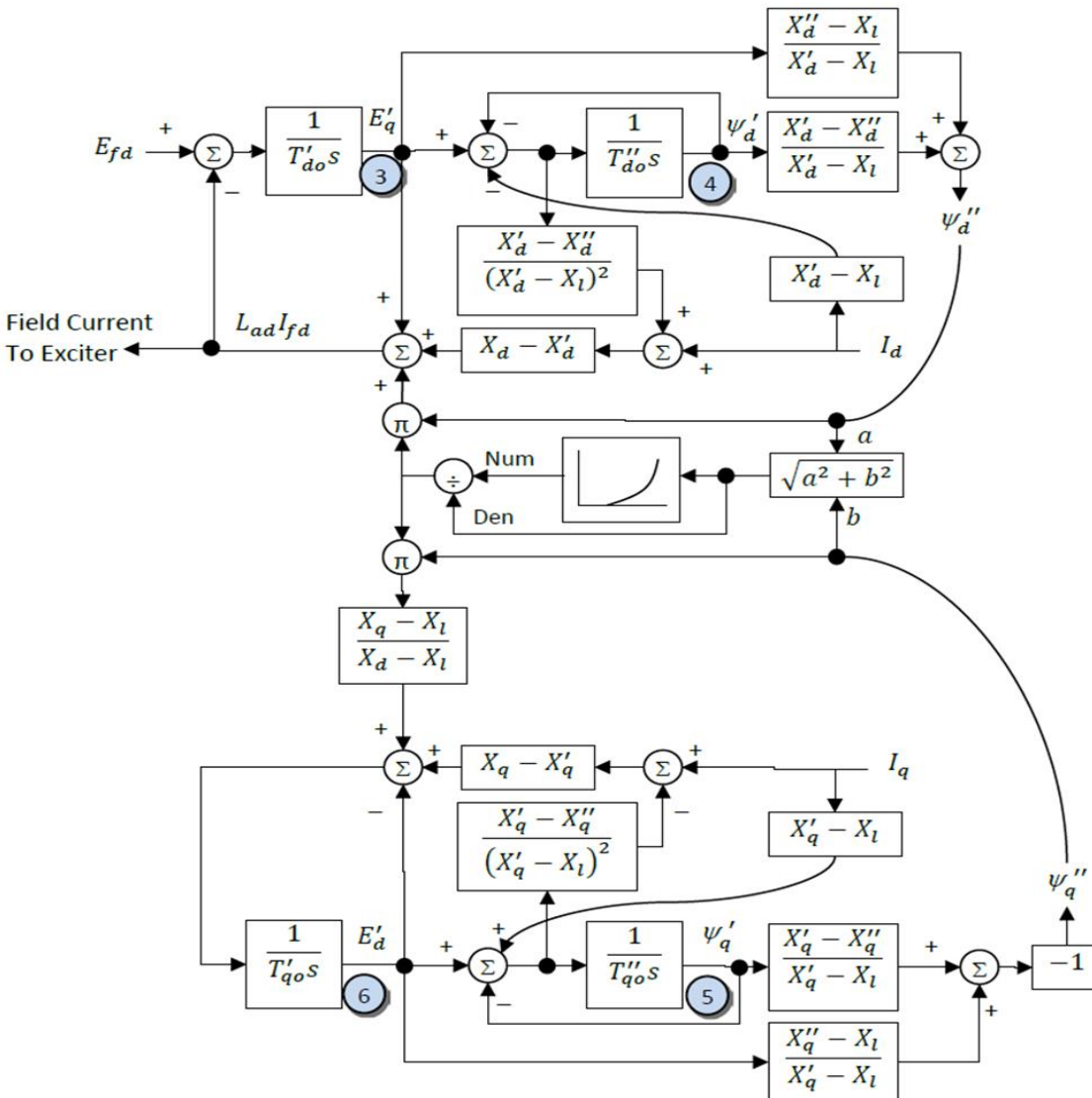
Saved as case **B4_GENSAL_SAT**

GENROU



- The GENROU model has been widely used to model round rotor machines
- Saturation is assumed to occur on both the d-axis and the q-axis, making initialization slightly more difficult

GENROU



The d-axis is similar to that of the GENSAL; the q-axis is now similar to the d-axis. Note that saturation now affects both axes.

GENROU Initialization



- Because saturation impacts both axes, the simple approach will no longer work
- Key insight for determining initial δ is that the magnitude of the saturation depends upon the magnitude of ψ'' , which is independent of δ

$$|\psi''| = |\bar{V} + (R_s + jX'')\bar{I}| \quad \text{This point is crucial!}$$

- Solving for δ requires an iterative approach; first get a guess of δ using the unsaturated approach

$$|E| \angle \delta = \bar{V} + (R_s + jX_q)\bar{I}$$

GENROU Initialization



- Then solve five nonlinear equations for five unknowns
 - The five unknowns are δ , E'_q , E'_d , ψ'_q , and ψ'_d
- Five equations come from the terminal power flow constraints (which allow us to define ψ_d and ψ_q as a function of the power flow voltage, current and δ) and from the differential equations initially set to zero
 - The ψ_d and ψ_q block diagram constraints
 - Two differential equations for the q-axis, one for the d-axis (the other equation is used to set the field voltage)
- Values can be determined using Newton's method, which is needed for the nonlinear case with saturation

GENROU Initialization



- Use dq transform to express terminal current as

$$\begin{bmatrix} I_d \\ I_q \end{bmatrix} = \begin{bmatrix} \sin \delta & -\cos \delta \\ \cos \delta & \sin \delta \end{bmatrix} \begin{bmatrix} I_r \\ I_i \end{bmatrix}$$

These values will change during the iteration as δ changes

- Get expressions for ψ''_q and ψ''_d in terms of the initial terminal voltage and δ

- Use dq transform to express terminal voltage as

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = \begin{bmatrix} \sin \delta & -\cos \delta \\ \cos \delta & \sin \delta \end{bmatrix} \begin{bmatrix} V_r \\ V_i \end{bmatrix}$$

Recall $X_d'' = X_q'' = X''$
and $\omega = 1$ (in steady-state)

- Then from $-\psi''_q + j\psi''_d = (V_d + jV_q) + (R_s + jX'')(I_d + jI_q)$

$$-\psi''_q = V_d + R_s I_d - X'' I_q$$

$$\psi''_d = V_q + R_s I_q + X'' I_d$$

Expressing complex equation as two real equations

GENROU Initialization Example



- Extend the two-axis example
 - For two-axis assume $H = 3.0$ per unit-seconds, $R_s = 0$, $X_d = 2.1$, $X_q = 2.0$, $X'_d = 0.3$, $X'_q = 0.5$, $T'_{do} = 7.0$, $T'_{qo} = 0.75$ per unit using the 100 MVA base.
 - For subtransient fields assume $X''_d = X''_q = 0.28$, $X_1 = 0.13$, $T''_{do} = 0.073$, $T''_{qo} = 0.07$
 - for comparison we'll initially assume no saturation
- From two-axis get a guess of δ

$$\bar{E} = 1.0946 \angle 11.59^\circ + (j2.0)(1.052 \angle -18.2^\circ) = 2.814 \angle 52.1^\circ$$

$$\rightarrow \delta = 52.1^\circ$$

Saved as case **B4_GENROU_NoSat**

GENROU Initialization Example



- And the network current and voltage in dq reference

$$\begin{bmatrix} V_d \\ V_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.0723 \\ 0.220 \end{bmatrix} = \begin{bmatrix} 0.7107 \\ 0.8326 \end{bmatrix}$$

$$\begin{bmatrix} I_d \\ I_q \end{bmatrix} = \begin{bmatrix} 0.7889 & -0.6146 \\ 0.6146 & 0.7889 \end{bmatrix} \begin{bmatrix} 1.000 \\ -0.3287 \end{bmatrix} = \begin{bmatrix} 0.9909 \\ 0.3553 \end{bmatrix}$$

- Which gives initial subtransient fluxes (with $R_s=0$),

$$\left(-\psi_q'' + j\psi_d''\right)\omega = \left(V_d + jV_q\right) + \left(R_s + jX''\right)\left(I_d + jI_q\right)$$

$$-\psi_q'' \omega = V_d + R_s I_d - X'' I_q = 0.7107 - 0.28 \times 0.3553 = 0.611$$

$$\psi_d'' \omega = V_q + R_s I_q + X'' I_d = 0.8326 + 0.28 \times 0.9909 = 1.110$$

GENROU Initialization Example



- Without saturation this is the exact solution

Initial values are:

$$\delta = 52.1^\circ,$$

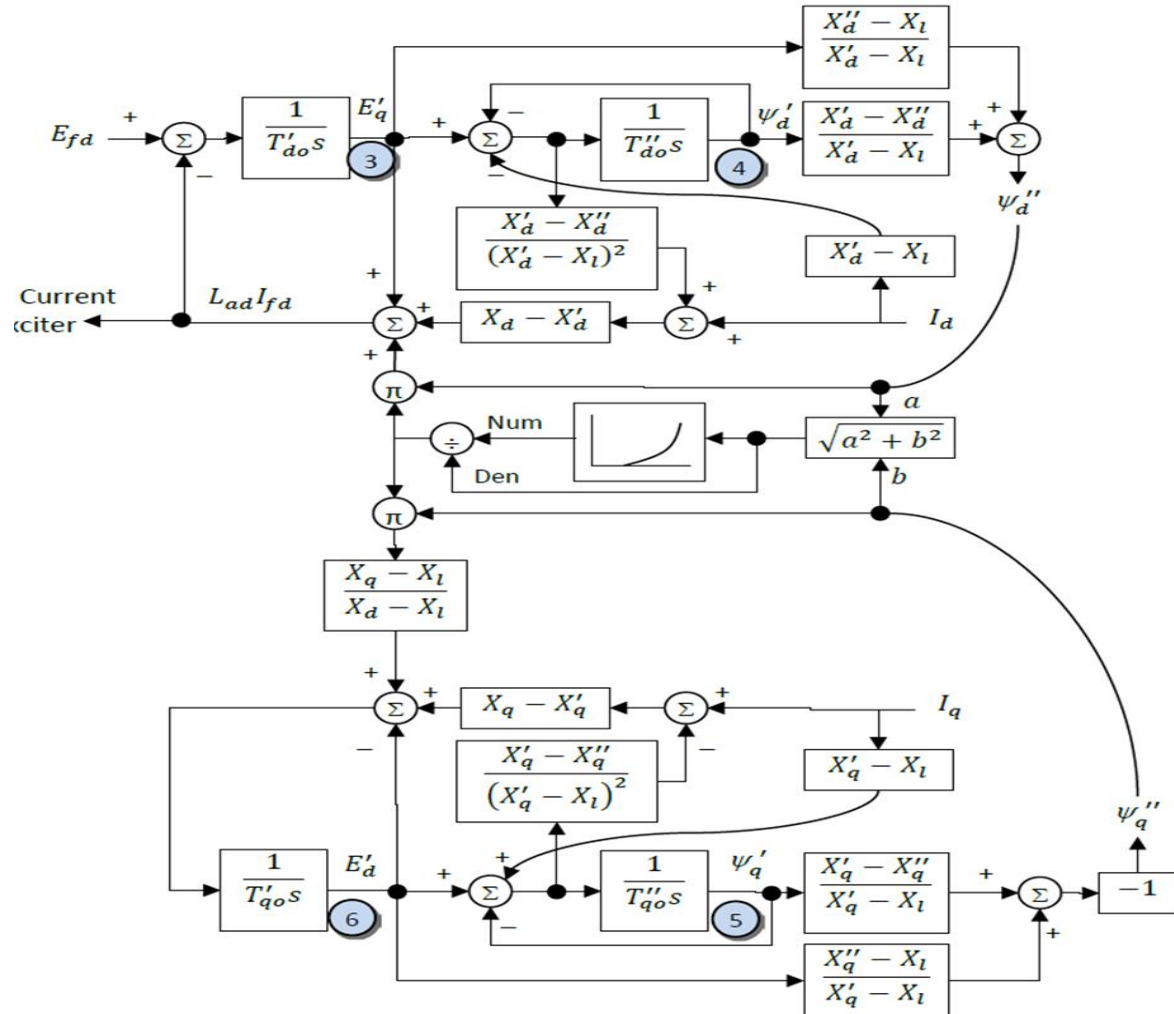
$$E'_q = 1.1298,$$

$$E'_d = 0.533,$$

$$\psi'_q = 0.6645,$$

$$\text{and } \psi'_d = 0.9614$$

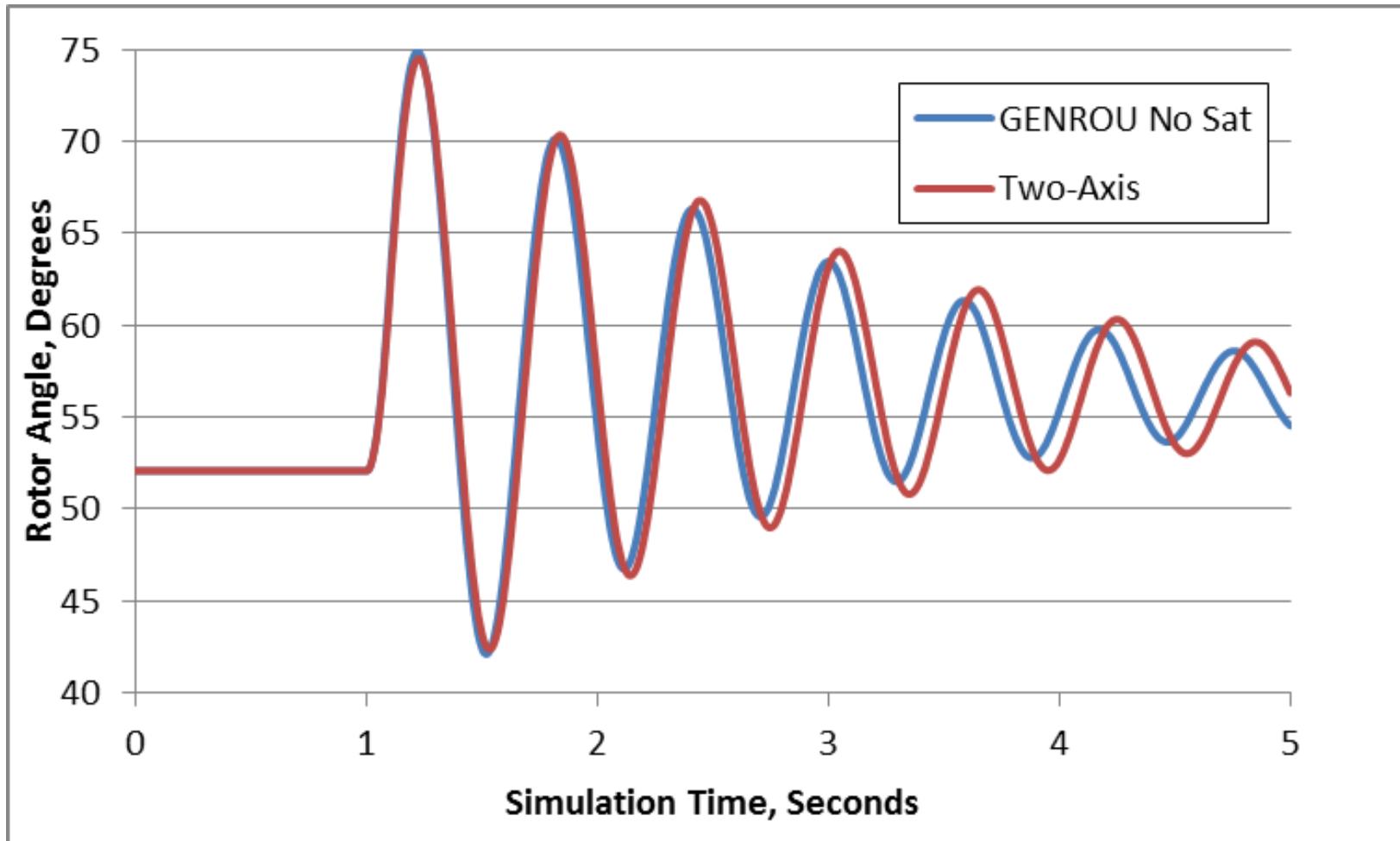
$$E_{fd} = 2.9133$$



Two-Axis versus GENROU Response



Figure compares rotor angle for bus 3 fault, cleared after 0.1 seconds



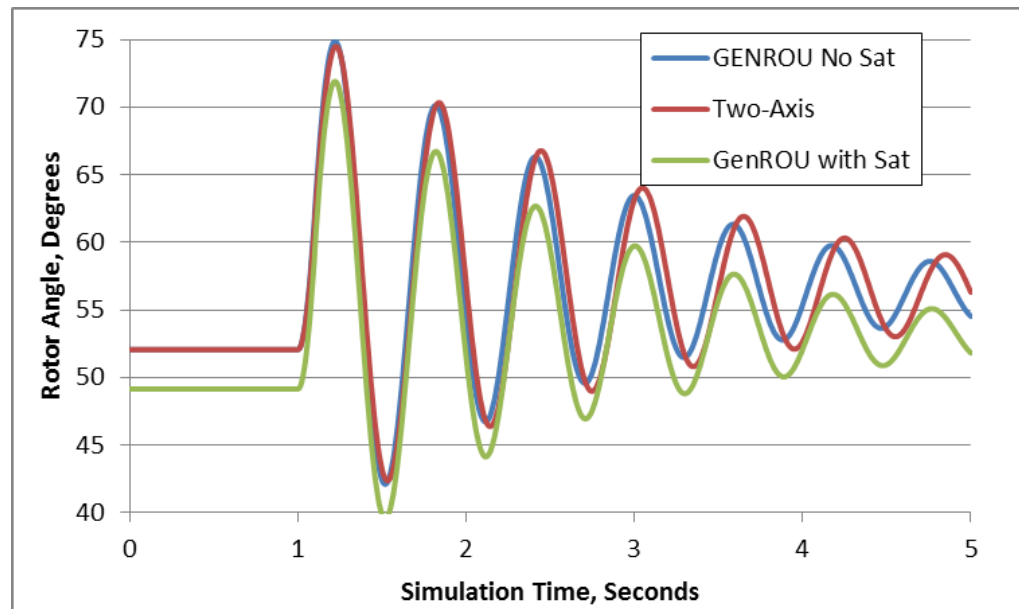
GENROU with Saturation



- Nonlinear approach is needed in common situation in which there is saturation
- Assume previous GENROU model with $S(1.0) = 0.05$, and $S(1.2) = 0.2$.
- Initial values are: $\delta = 49.2^\circ$, $E'_q = 1.1591$, $E'_d = 0.4646$, $\psi'_q = 0.6146$, and $\psi'_d = 0.9940$
- $E_{fd} = 3.2186$

Same fault as before

Saved as case
B4_GENROU_Sat



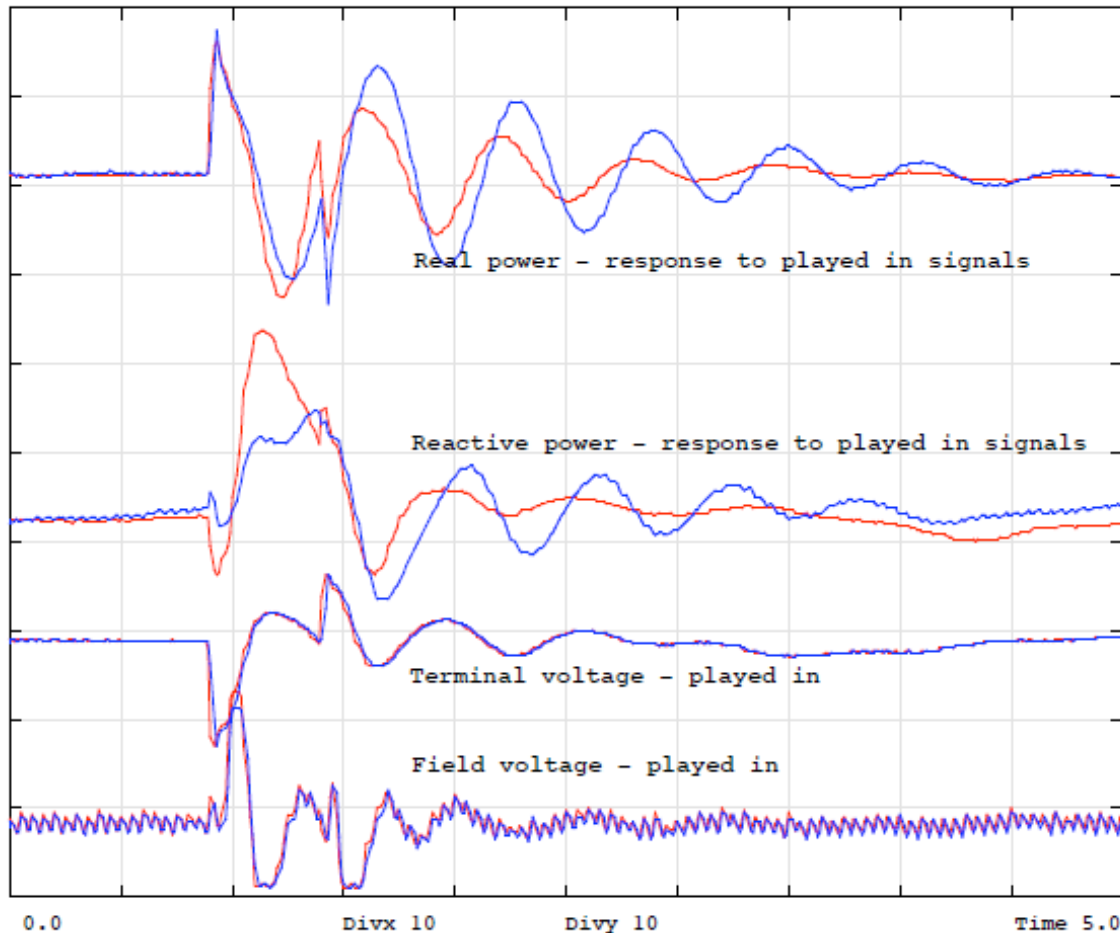
GENTPF and GENTPJ Models



- These models were introduced in 2009 to provide a better match between simulated and actual system results for salient pole machines
 - Desire was to duplicate functionality from old BPA TS code
 - Allows for subtransient saliency ($X''_d \neq X''_q$)
 - Can also be used with round rotor, replacing GENSAL and GENROU
- Useful reference is available at below link; includes all the equations, and saturation details

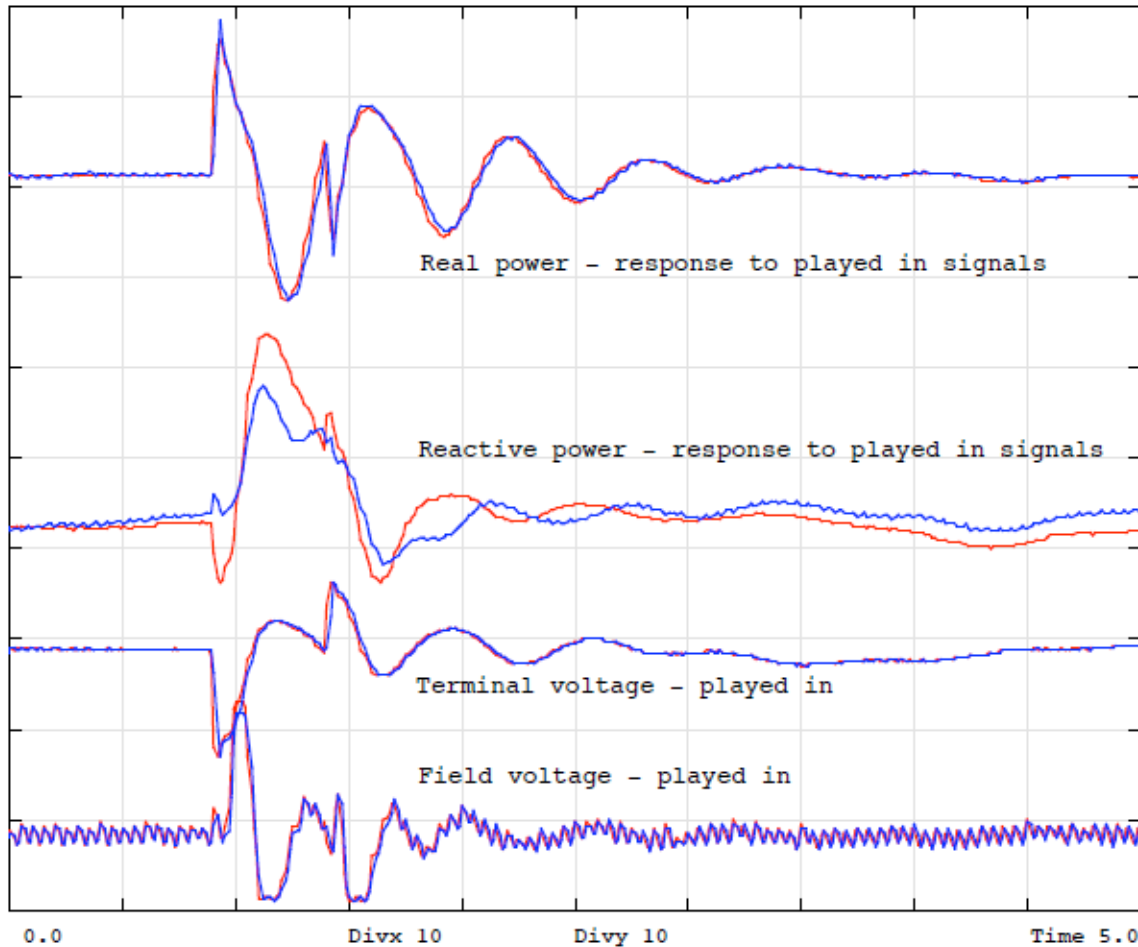
<https://www.wecc.biz/Reliability/gentpj-typej-definition.pdf>

Motivation for the Change: GENSAL Actual Results



Chief Joseph
disturbance
playback
GENSAL
BLUE = MODEL
RED = ACTUAL
(Chief Joseph is a
2620 MW hydro
plant on the
Columbia River in
Washington)

GENTPJ Results



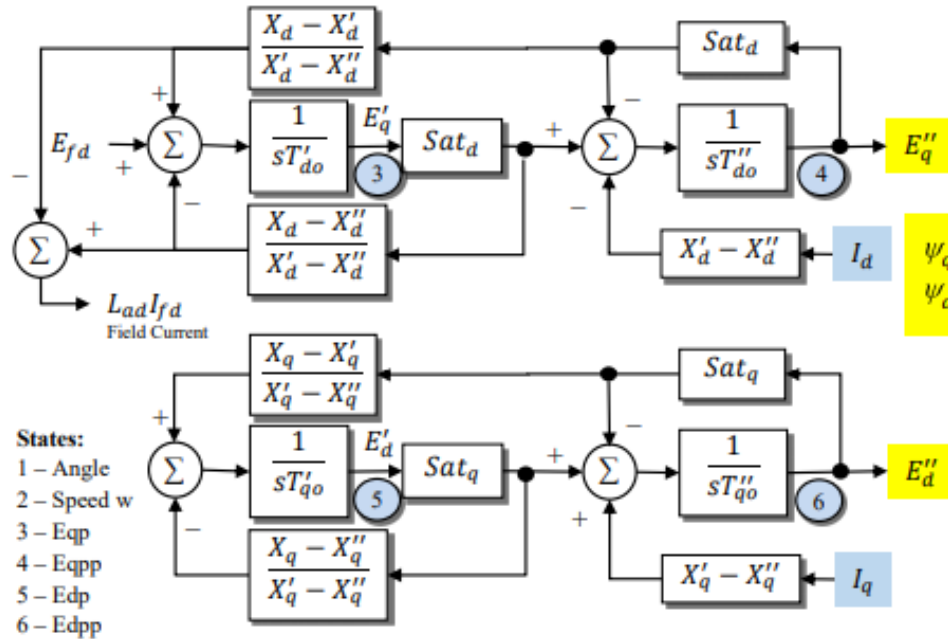
Chief Joseph
disturbance
playback

GENTPJ

BLUE = MODEL

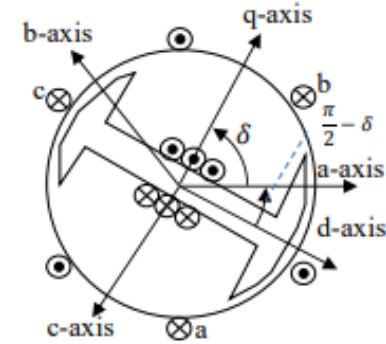
RED = ACTUAL

GENTPF and GENTPJ Models



$$\psi_q'' = -E_d''$$

$$\psi_d'' = +E_q''$$



Most of WECC machine models are now GENTPF or GENTPJ

Mechanical Swing Equations

- 1 $\dot{\delta} = \omega * \omega_0$
- 2 $\dot{\omega} = \frac{1}{2H} \left(\frac{P_{mech} - D\omega}{1 + \omega} - T_{elec} \right)$

ω = per unit speed deviation, so $\omega = 0$ means we are at synchronous speed and $\omega = 1$ would mean it's spinning at double synchronous speed
 ω_0 = synchronous speed $2\pi f_0$ where f_0 is the nominal system frequency in Hz

Note: If option *Ignore Speed Effects in Generator Swing Equation* is true, then instead use

$$\dot{\omega} = \frac{1}{2H} (P_{mech} - D\omega - T_{elec})$$

$$\psi_{ag} = \sqrt{(V_{qterm} + I_q R_a + I_d X_l)^2 + (V_{dterm} + I_d R_a - I_q X_l)^2}$$

D-Axis: $Sat_d = 1 + \text{SaturationFunction} \left(\psi_{ag} + K_{is} \sqrt{I_d^2 + I_q^2} \right)$

Q-Axis: $Sat_q = 1 + \frac{X_q}{X_d} \text{SaturationFunction} \left(\psi_{ag} + K_{is} \sqrt{I_d^2 + I_q^2} \right)$

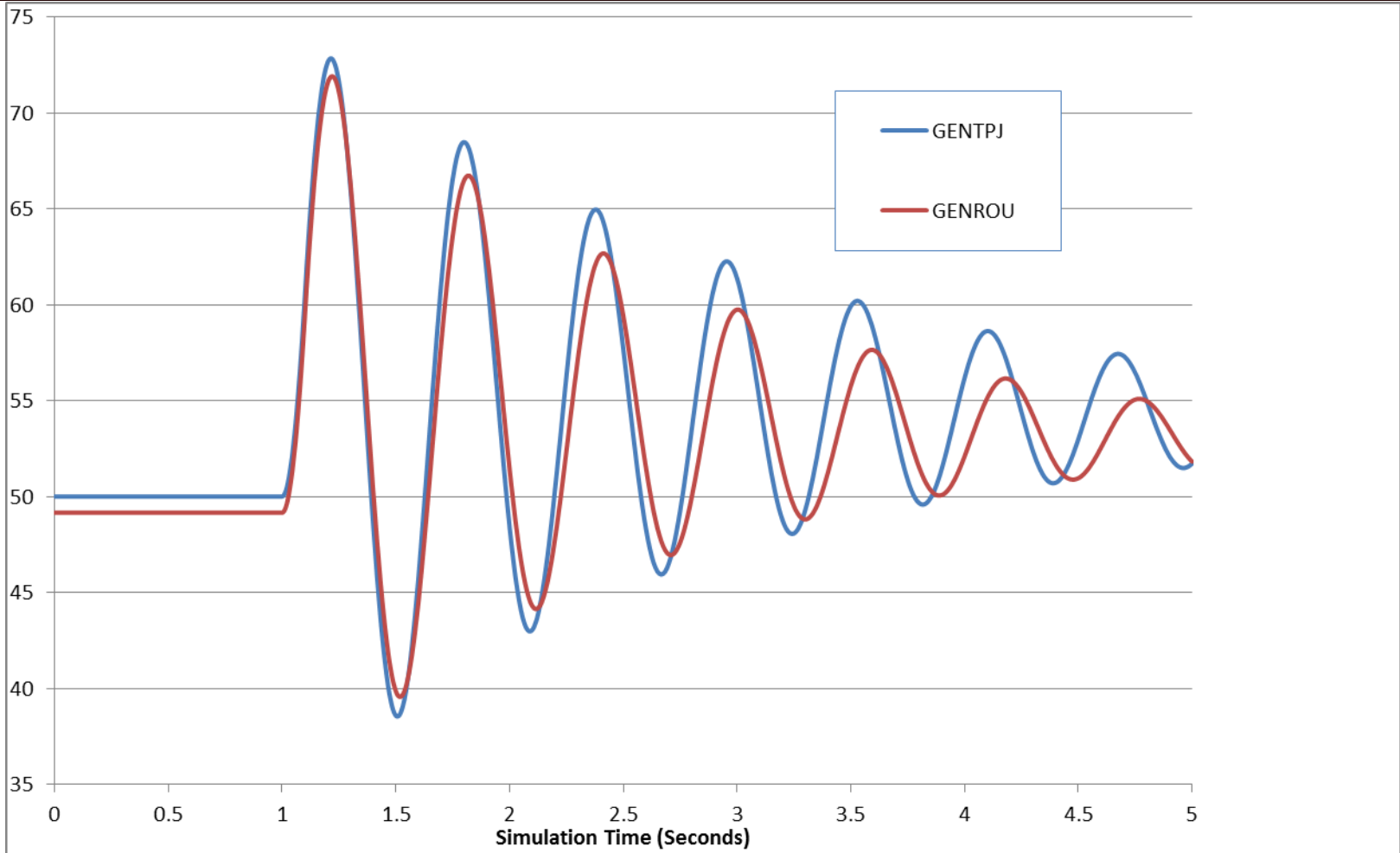
If nonzero, K_{is} typically ranges from 0.02 to 0.12

Theoretical Justification for GENTPF and GENTPJ



- In the GENROU and GENSAL models saturation shows up purely as an additive term of E_q' and E_d'
 - Saturation does not come into play in the network interface equations and thus with the assumption of $X_q''=X_d''$ a simple circuit model can be used
- The advantage of the GENTPF/J models is saturation really affects the entire model, and in this model it is applied to all the inductance terms simultaneously
 - This complicates the network boundary equations, but since these models are designed for $X_q'' \neq X_d''$ there is no increase in complexity

GENROU/GENTPJ Comparison

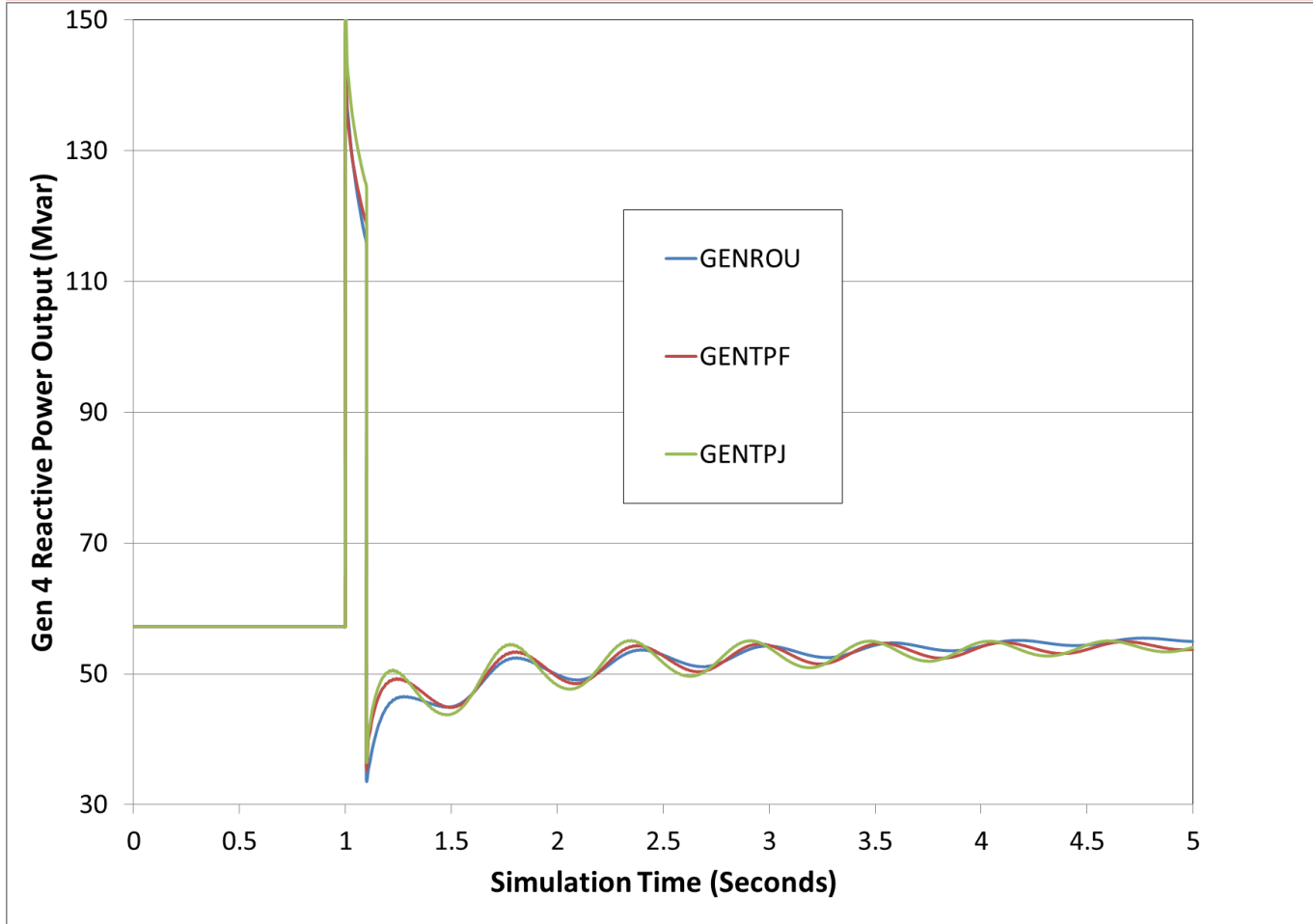


Saved as case **B4_GENTPJ_Sat**

GENROU, GenTPF, GenTPJ



Figure compares gen 4 reactive power output for the 0.1 second fault



Why does this even matter?



- GENROU and GENSAL models date from 1970, and their purpose was to replicate the dynamic response the synchronous machine
 - They have done a great job doing that
- Weaknesses of the GENROU and GENSAL model has been found to be with matching the field current and field voltage measurements
 - Field Voltage/Current may have been off a little bit, but that didn't effect dynamic response
 - It just shifted the values and gave them an offset
- Shifted/Offset field voltage/current didn't matter too much in the past

Over and Under Excitation Limiters



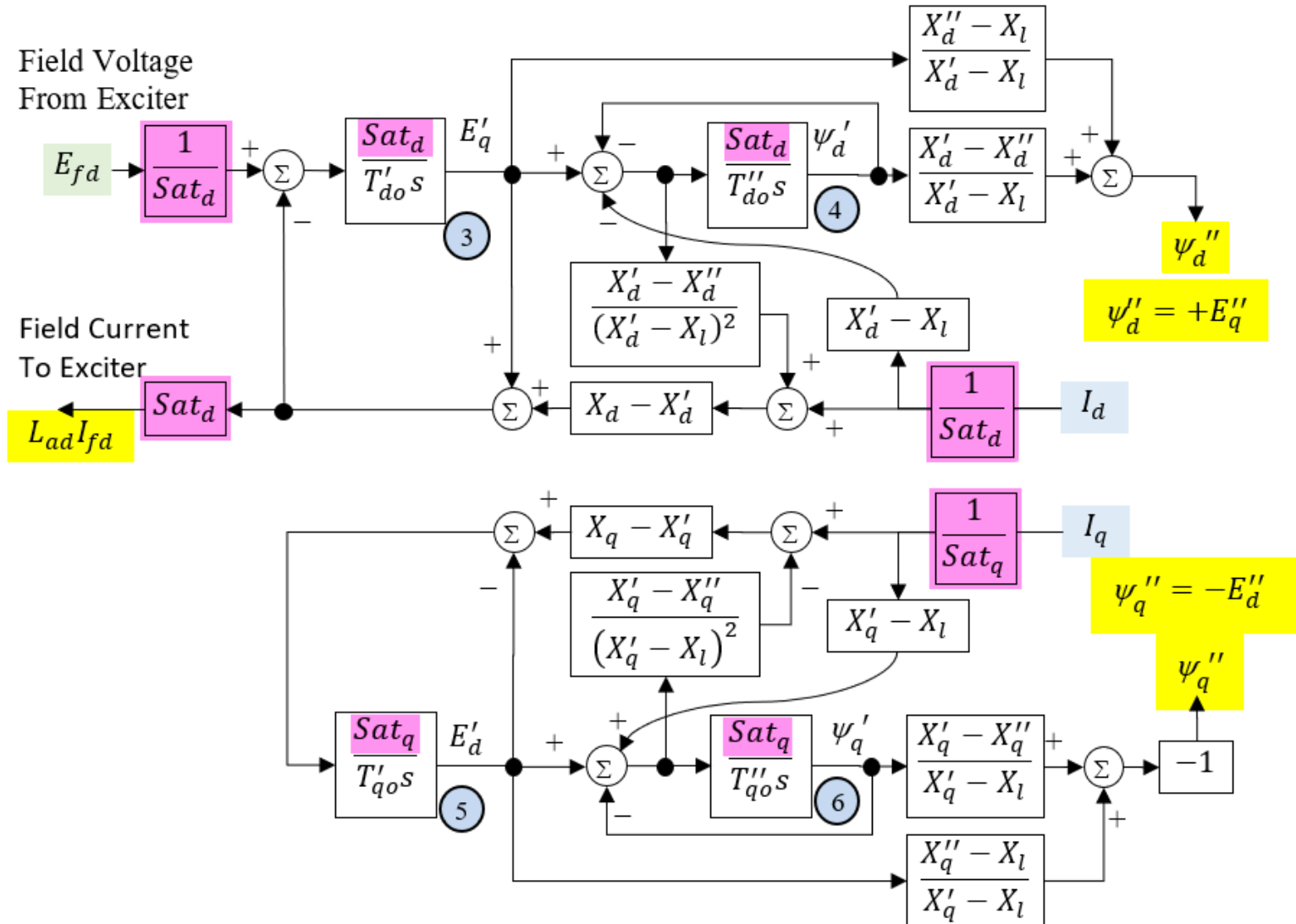
- Traditionally our industry has not modeled over excitation limiters (OEL) and under excitation limiters (UEL) in transient stability simulation
 - The Mvar outputs of synchronous machines during transients likely do go outside these bounds in our existing simulations
 - Our Simulation haven't been modeling limits being hit anyway, so the overall dynamic response isn't impacted
- If the industry wants to start modeling OEL and UEL, then we need to better match the field voltage and currents
 - Otherwise we're going to be hitting these limits when in real life we are not

GENTPW, GENQEC



- New models are under development that address several issues
 - Saturation function should be applied to all input parameters by multiplication
 - This also ensures a conservative coupling field assumption of Peter W. Sauer paper from 1992
 - Same multiplication should be applied to both d-axis and q-axis terms (assume same amount of saturation on both)
- Results in differential equations that are nearly the same as GENROU
 - Scales the inputs and outputs, and effects time constants
- Network Interface Equation is same as GENTPF/J

GENTPW and GENQEC Basic Diagram



GENQEC Specification

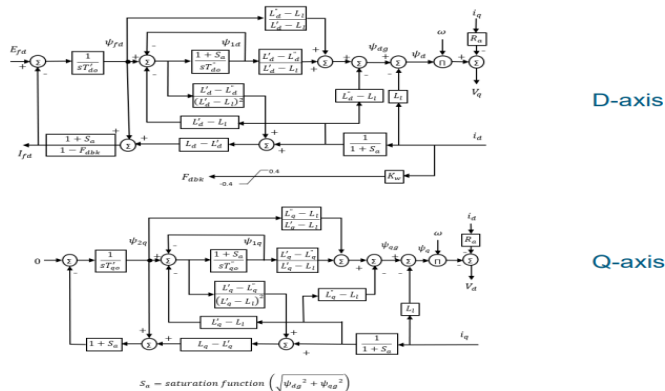


- If you are interested in seeing the GENQEC specification (on Revision 3 as of 11/9/20), it is available at

www.wecc.org/Reliability/GENQEC%20Model%20Specification%20-%20R3.pdf

www.wecc.org/Administrative/Wang%20-%20GENQEC%20Model%20Overview.pdf
<https://www.wecc.org/Administrative/Wang%20-%20GENQEC%20Model%20Overview.pdf>

GENQEC Block Diagram



The GENQEC is implemented in PowerWorld

Comment about all these Synchronous Machine Models



- The models are improving. However, this does not mean the old models were useless
- All these models have the same input parameter names, but that does not mean they are exactly the same
 - Input parameters are tuned for a particular model
 - It is NOT appropriate to take all the parameters for GENROU and just copy them over to a GENTPJ model and call that your new model
 - When performing a new generator testing study, that is the time to update the parameters